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**Exclusive charmless
semileptonic B decays and
 $|V_{ub}|$ measurement in BaBar**

Torino, 08/01/2003

OUTLINE



- ◆ Physics Motivations
 - CKM matrix determination
- ◆ Measurement of $|V_{ub}|$
 - Experimental approaches
 - Inclusive Recoil technique
 - Exclusive $B \rightarrow X_u | \nu$ decays
- ◆ Conclusions

CKM matrix (I)

- Weak processes with quark flavour change couple the boson vector field to the charged weak V-A current, containing elements of the Cabibbo-Kobayashi-Maskawa quark-mixing matrix.

$$\mathcal{J}^\mu = \sum_{i,j} \bar{u}_i \gamma^\mu \frac{1}{2}(1 - \gamma_5) V_{ij} d_j$$

$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

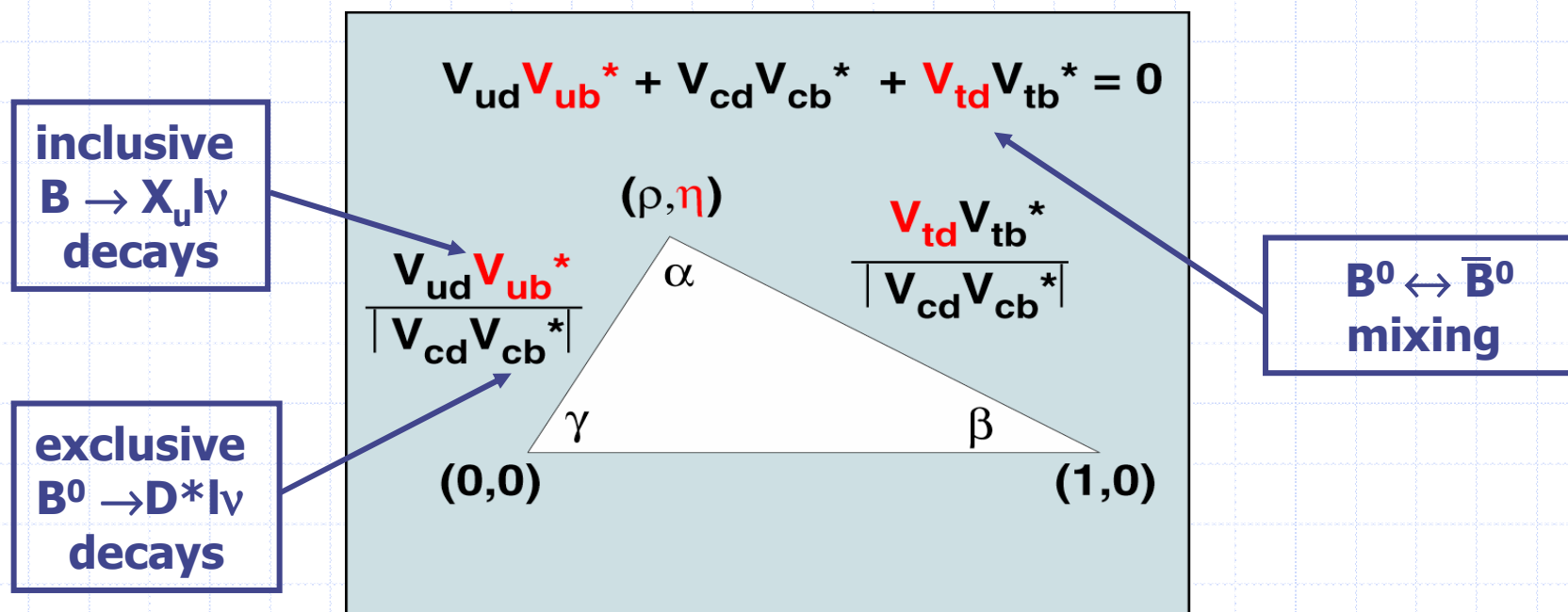
- With 3 quark generations there are 4 real independent parameters. The presence of an imaginary phase is responsible for CP violation.

$$\lambda = \sin\theta_c \cong 0.22$$

$$V = \begin{pmatrix} 1 - \frac{1}{2}\lambda^2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \frac{1}{2}\lambda^2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + \mathcal{O}(\lambda^4)$$

CKM Matrix (II)

- ◆ The unitarity of CKM matrix implies relations between its elements which can be expressed as “unitary triangles”, whose non-zero area accounts for CP violation.
- ◆ In 2001 BaBar established \overline{CP} in the B sector by measuring $\sin(2\beta)$.



CKM matrix elements

PDG 2002

| $ V_{xy} $ | Measured value | Total Error (%) | Tecnique |
|------------|--|-----------------|--|
| $ V_{ud} $ | 0.9734 ± 0.0008 | $< 0.1\%$ | Nuclear β Decays |
| $ V_{us} $ | 0.2196 ± 0.0026 | $\sim 1\%$ | K_{e3} Decay ($K^{+(0)} \rightarrow \pi^{0(-)} e^+ \nu_e$) |
| $ V_{ub} $ | 0.0036 ± 0.0007 | $\sim 20\%$ | Charmless SL B Decays |
| $ V_{cd} $ | 0.224 ± 0.016 | $\sim 7\%$ | Charm production with ν beams |
| $ V_{cs} $ | 0.996 ± 0.013 | $\sim 1\%$ | Charm-tagged W Decays |
| $ V_{cb} $ | 0.0412 ± 0.0020 | $\sim 5\%$ | Charmed SL B Decays |
| $ V_{td} $ | $ V_{tb}^* V_{td} = 0.0083 \pm 0.016$ | - | $B_d \bar{B}_d$ Mixing |
| $ V_{ts} $ | $ V_{td} / V_{ts} < 0.24$ | - | $B_s \bar{B}_s$ Mixing |
| $ V_{tb} $ | $ V_{tb} ^2 / \sum_{d,s,b} V_{ty} ^2 = 0.94 \pm 0.31$ | - | Semileptonic t Decays |

Constraints on the unitary triangle

- ◆ $|V_{ub}|$ and $|V_{cb}|$ give a constraint on the Unitary Triangle.
- ◆ Different experimental approaches exploited Inclusive and Exclusive Semileptonic B decays.
- ◆ BaBar improved measurements of $|V_{cb}|$ (published soon) and $|V_{ub}|$.

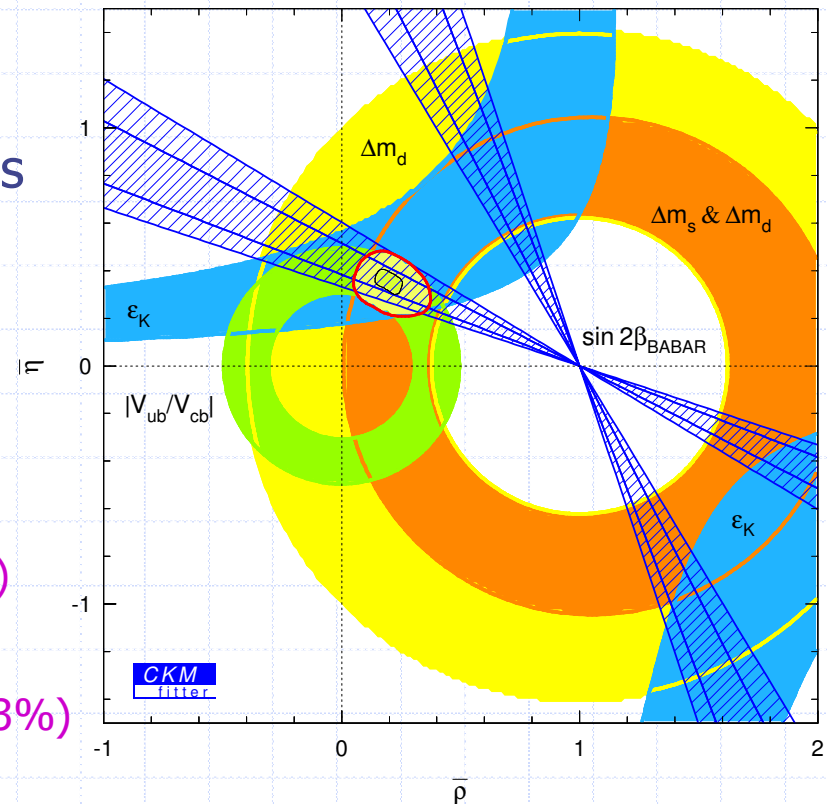
$$|V_{cb}| = (47.4 \pm 1.4 \pm 2.0 \pm 2.1) * 10^{-3} \quad (\sim 7\%)$$

(CLEO exclusive – hep-ex/0203032)

$$|V_{cb}| = (4.04 \pm 0.09 \pm 0.05 \pm 0.08) * 10^{-2} \quad (\sim 3\%)$$

(CLEO inclusive – PRL 87, 251808 (2001))

- ◆ $|V_{ub}|$ is the CKM matrix element with biggest uncertainty.



$|V_{ub}|$ from semileptonic B decays

◆ $|V_{ub}|$ can be extracted from charmless semileptonic B decays.

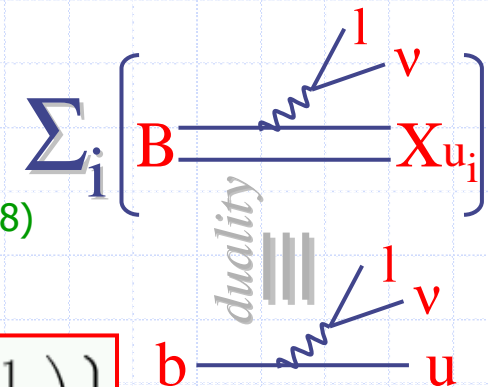
◆ Calculation of the total decay rate using OPE:

- N. Uraltsev, Int. J. Mod. Phys. A 14, 4641 (1999)

[arXiv:hep-ph/9905520]

- I.I. Bigi, R.D. Dikeman and N. Uraltsev, Eur. Phys. J. C 4, 453 (1998)

[arXiv:hep-ph/9706520]



$$\Gamma_{sl}^{b \rightarrow u} = \frac{G_F^2 m_b^5}{192 \pi^3} |V_{ub}|^2 \left\{ A_0 \left(1 - \frac{\mu_\pi^2 - \mu_G^2}{2m_b^2} \right) - 2 \frac{\mu_G^2}{m_b^2} + O\left(\frac{1}{m_b^3}\right) \right\}$$

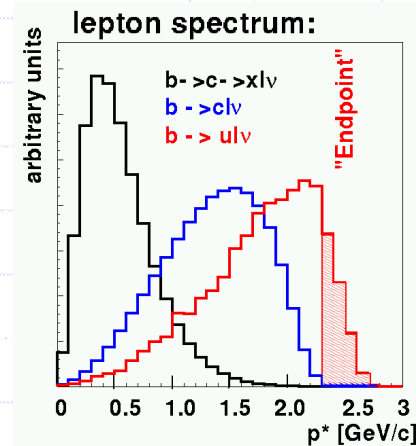
◆ Hadronization effects and Fermi motion must be taken into account.

◆ Main background is from $B \rightarrow X_c | \nu$ events ($\text{BR}(b \rightarrow c | \nu) = \sim 60 \times \text{BR}(b \rightarrow u | \nu)$), can be controlled only in limited regions of phase space (endpoint of the lepton spectrum).

Experimental approaches

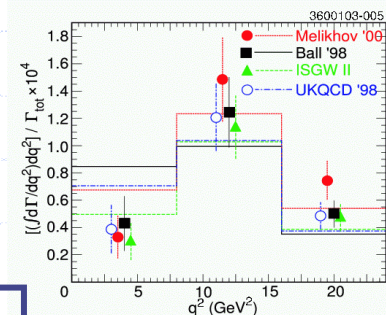
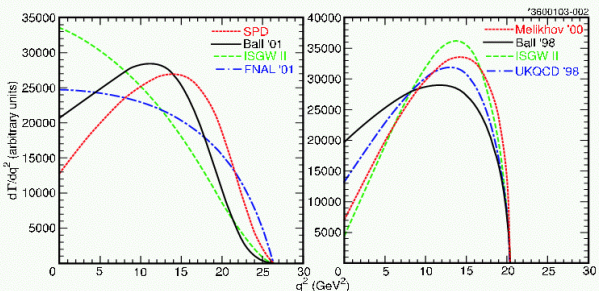
◆ Measure the lepton

- Basic approach for all analysis
- Endpoint of lepton spectrum ($p^* > 2.3 \text{ GeV}$)
- 10-15% of $b \rightarrow u \ell \nu$ phase space accepted
- Shape function information (e.g. from $b \rightarrow s \gamma$)



◆ Reconstruct the neutrino kinematics

- Low experimental efficiency ($\sim 5\%$)
- Higher phase space acceptance (20-30%)
- Large background from $b \rightarrow c \ell \nu$ and continuum
- Modest ν momentum resolution ($\sigma \sim 0.5 \text{ GeV}$)
- Dependence from m_b and resonant states modeling

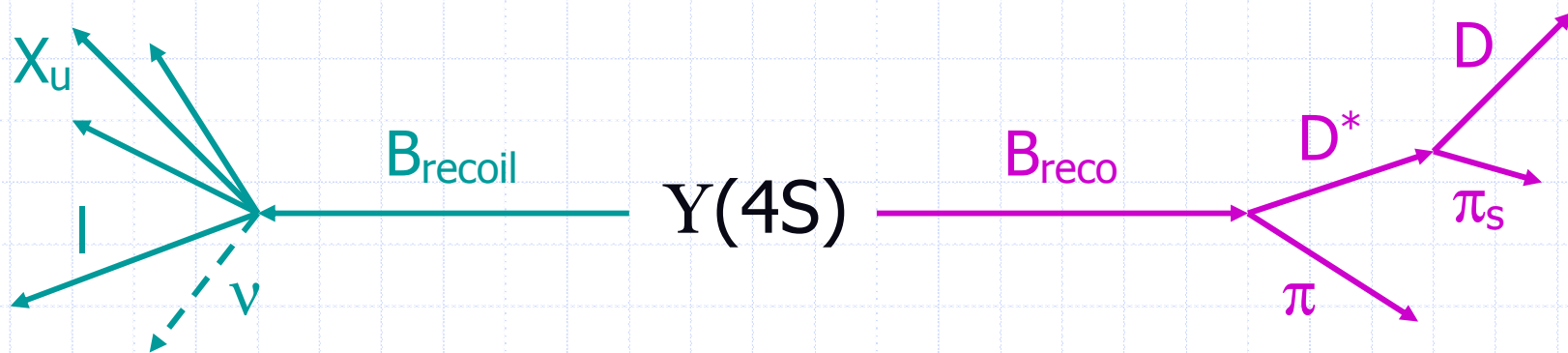


$$q^2 = (p_{\text{lep}} + p_{\nu})^2$$

◆ Reconstruct the other B...

RECOIL technique (I)

- ◆ This analysis uses $Y(4S) \rightarrow B\bar{B}$ events in which one B meson is fully reconstructed (B_{reco}) and the semileptonic decay of the recoiling B (B_{recoil}) is identified by the presence of a high energy lepton (e or μ).
- ◆ Since there are no missing particles on the B_{reco} side, the rest of the event comes from the B_{recoil} .
- ◆ This is equivalent to having a **single B beam!**

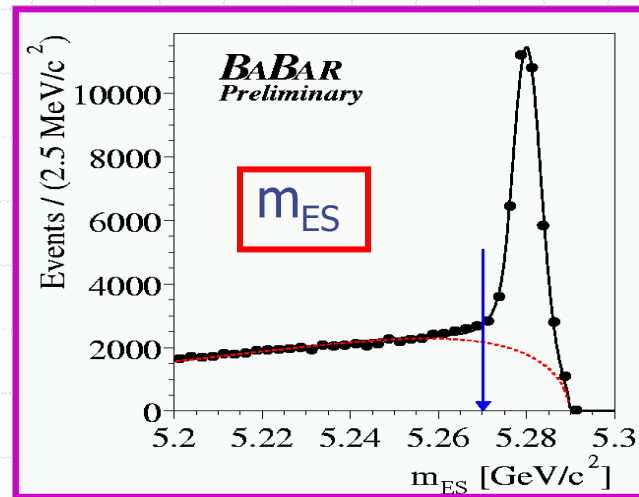


RECOIL technique (II)

$$m_{ES} = \sqrt{E_{beam}^{*2} - p_B^{*2}}$$

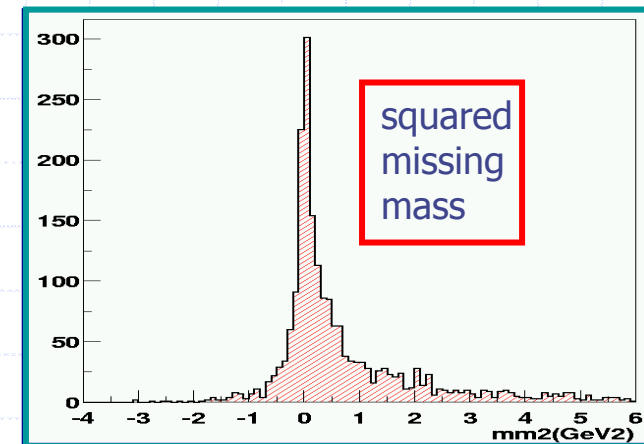
B_{reco}

- ◆ Clean sample with small background
- ◆ B_{reco} (B_{recoil}) **flavor tagging**
- ◆ Small reconstruction efficiency: $\sim 0.4\%$



B_{recoil}

- ◆ M_x reconstruction
- ◆ Lepton charge – B_{reco} flavour correlation
- ◆ **Missing mass can be determined**



Semi-Exclusive B_{reco} reconstruction

◆ B_{reco} mesons reconstructed with **Semi-Exclusive** technique:

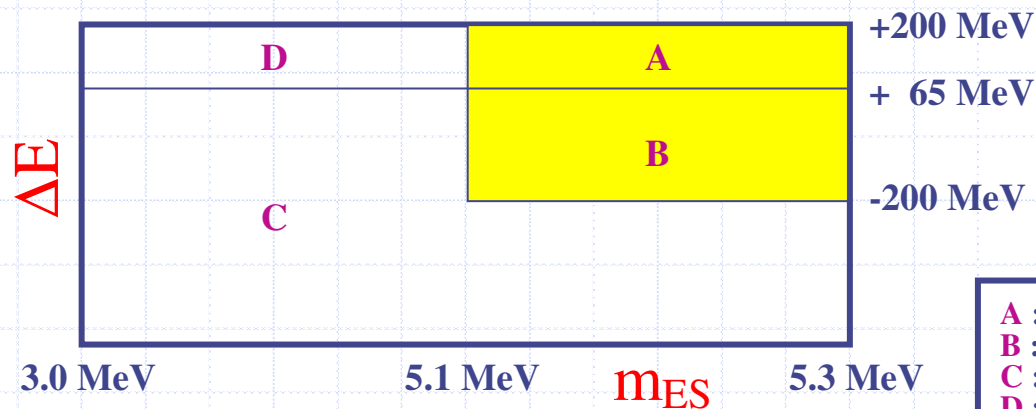
$$B \rightarrow D^{(*)} X$$

$$X = n\pi \ mK \ pK_s \ q\pi^0 \ (n+m+p+q < 6)$$

◆ Breco candidates selected in $(\Delta E, m_{\text{ES}})$ plane:

- D modes reconstructed and **combined with a h** (π or K)
- Added a couple h^+h^- , a π^0 or a $4h^\pm$ system, up to max 7 particles or two neutrals in X.

| mode | Branching Fraction (%) |
|---------------------------------------|------------------------|
| $B \rightarrow D^{*-} X$ | 22.7 ± 1.6 |
| $B \rightarrow D^- X$ | 24.1 ± 1.9 |
| $B \rightarrow \bar{D}^0 X$ | 26.0 ± 2.7 |
| $B \rightarrow \bar{D} X$ | 63.5 ± 2.9 |
| $B \rightarrow D_s^+ X$ | 10.0 ± 2.5 |
| $B^0 \rightarrow D^{\pm(*)} l \nu$ | 6.7 ± 0.3 |
| $B^- \rightarrow D^{0(*)} l \nu$ | 7.7 ± 0.8 |
| $B^0 \rightarrow D^{-(*)} D^{+(*)}$ | ~ 0.3 |
| $B^0 \rightarrow D^{-(*)} D^{+(*)} K$ | ~ 1.0 |
| $B^0 \rightarrow D^{-(*)} D_s^{(*)}$ | 4.8 ± 1.0 |
| $B^+ \rightarrow D^{0(*)} D^{+(*)}$ | ~ 0.3 |
| $B^+ \rightarrow D^{0(*)} D^{+(*)} K$ | ~ 1.0 |
| $B^+ \rightarrow D^{0(*)} D_s^{(*)}$ | 4.8 ± 1.2 |



$$m_{\text{ES}} = \sqrt{E_{\text{beam}}^{*2} - p_B^{*2}}$$

$$\Delta E = E_B^* - E_{\text{beam}}^*$$

A : only used as a candidate
B : used as a candidate and as a seed
C : only used as a seed
D : not used

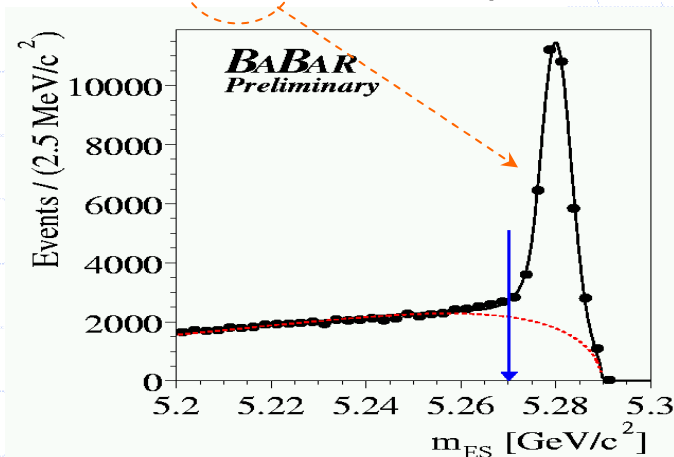
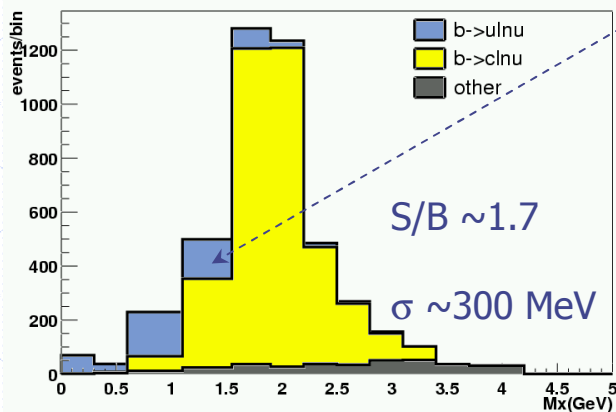
Analysis of B_{recoil}

- ◆ B_{recoil} selection and reconstruction of the X system in $B \rightarrow X_u l \nu$ (in the region $M_x < 1.55 \text{ GeV}/c^2$):
 - One and only one lepton with $p^* > 1 \text{ GeV}$
 - Correlation between lepton charge and B_{reco} flavour (included correction for B^0 mixing)
 - $M_{\text{miss}}^2 < 0.5 \text{ GeV}^2/c^4$
 - Charge conservation: $Q_{\text{tot}}=0$
 - Kinematic fit (2-C): improve hadronic mass resolution
- ◆ Separate $B \rightarrow X_u l \nu$ in two samples:
 - Signal enriched (veto on K^\pm and K_s): used to perform the measurement
 - Signal depleted (no Kaon veto): used as control sample

Extraction of BR($b \rightarrow ul\nu$)

- ◆ Fit on the signal enhanced sample
- ◆ Components in the M_X distribution fit: **$b \rightarrow ul\nu$** , **$b \rightarrow cl\nu$** , **background**
- ◆ Signal efficiency ($\epsilon_{sel}^u \epsilon_{M_X}^u$), B_{reco} efficiency ratio ($\epsilon_t^u / \epsilon_t^{sl}$) and lepton efficiency ratio ($\epsilon_l^u / \epsilon_l^{sl}$) from MC

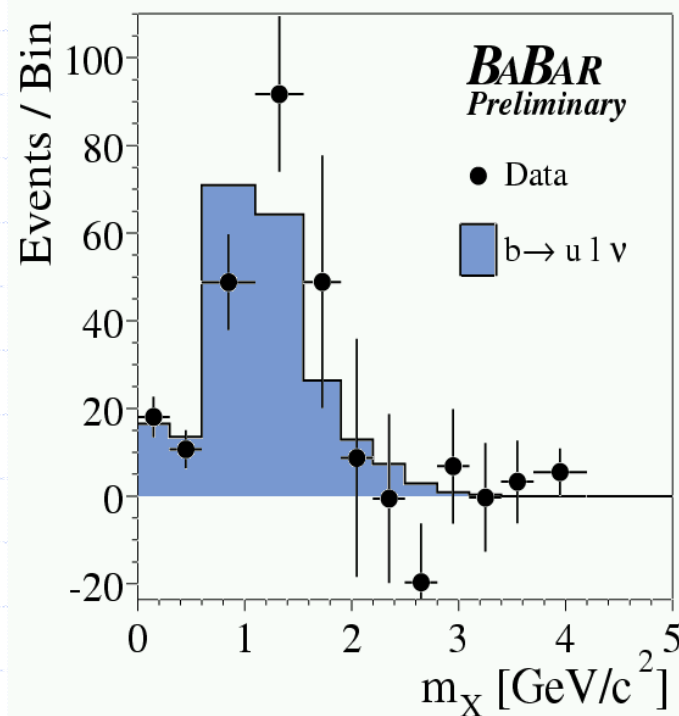
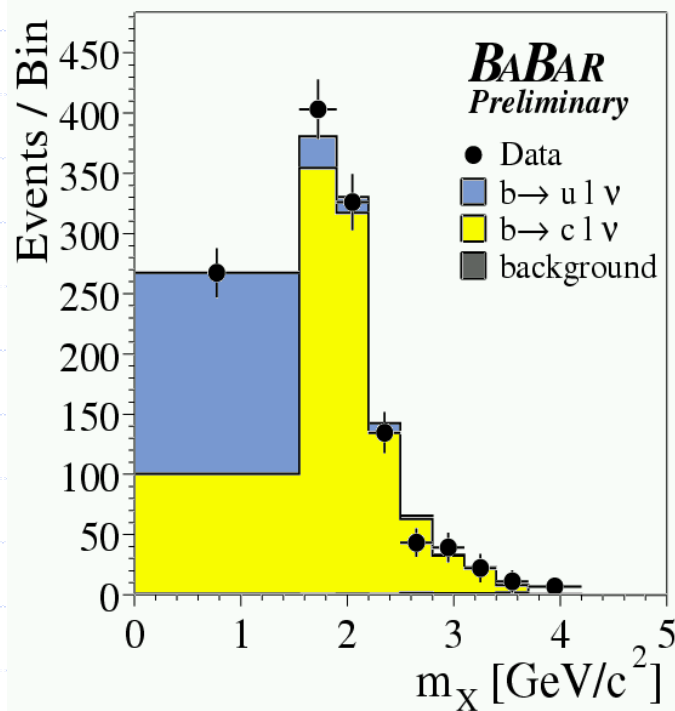
$$R_{u/sl} = \frac{\mathcal{B}(B \rightarrow X_{ul}\nu)}{\mathcal{B}(B \rightarrow X_{l\nu})} = \frac{N_{true}^u}{N_{true}^{sl}} = \frac{N_u / (\epsilon_{sel}^u \epsilon_{M_X}^u)}{N_{sl}} \times \frac{\epsilon_l^{sl} \epsilon_t^{sl}}{\epsilon_l^u \epsilon_t^u}$$



- ◆ Multiply by total semileptonic Branching Ratio measured by BaBar:

$$\mathcal{B}(B \rightarrow X e \nu) = (10.87 \pm 0.18 \pm 0.30)\%$$

Inclusive Branching Ratio



82 fb⁻¹

$$R_{u/sl} = \frac{\mathcal{B}(B \rightarrow X_u l \bar{\nu})}{\mathcal{B}(B \rightarrow X l \bar{\nu})} = 0.0206 \pm 0.0025(\text{stat}) \pm 0.0009(\text{MC stat}) \pm 0.0023(\text{syst}) \pm 0.0036(\text{theo})$$

$|V_{ub}|$ result

Submitted to PRL
hep-ex/0307062

- ◆ The measured charmless semileptonic branching ratio is:

$$\mathcal{B}(B \rightarrow X_u \ell \bar{\nu}) = (2.24 \pm 0.27(stat) \pm 0.26(syst) \pm 0.39(theo))$$

- ◆ $|V_{ub}|$ can be extracted using the relation: $\tau_b = 1.608 \pm 0.016$ ps (PDG02)
 $m_b = 4.58 \pm 0.09$ GeV

$$|V_{ub}| = 0.00445 \left(\frac{\mathcal{B}(B \rightarrow X_u \ell \nu)}{0.002} \frac{1.55 ps}{\tau_b} \right)^{1/2} \times (1.0 \pm 0.020_{pert} \pm 0.052_{1/m_b^3})$$

- ◆ The value for $|V_{ub}|$ from the inclusive data sample (in OPE approximation) is:

$$|V_{ub}| = (4.62 \pm 0.28(stat) \pm 0.27(syst) \pm 0.40(theo) \pm 0.09(pert) \pm 0.24(1/m_b^3)) \times 10^{-3}$$

Summary of $|V_{ub}|$ measurements

◆ Inclusive recoil technique allows for a $|V_{ub}|$ measurement with relative total error better than LEP average.

◆ Previous BaBar $|V_{ub}|$ measurements

- Exclusive $B \rightarrow \rho e \nu$

(hep-ex/0301001)

$$|V_{ub}| = (3.29 \pm 0.42_{\text{stat}} \pm 0.47_{\text{syst}} \pm 0.60_{\text{theo}}) * 10^{-3}$$

- Inclusive electron spectrum endpoint

(hep-ex/0207081)

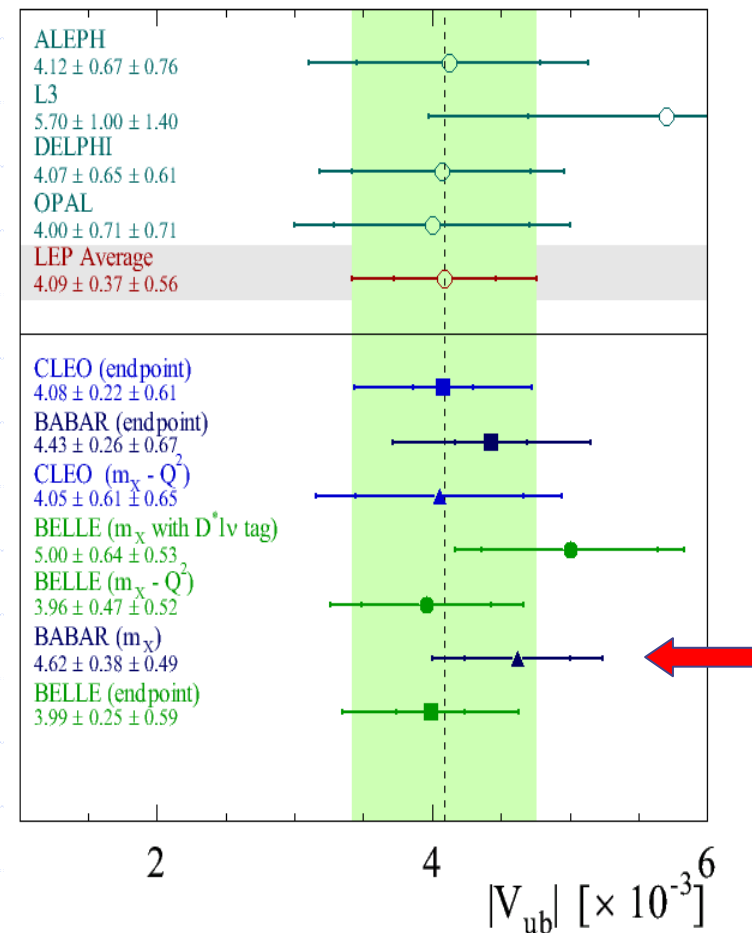
$$|V_{ub}| = (4.43 \pm 0.29_{\text{stat}} \pm 0.25_{\text{exp}} \pm 0.50_{\text{fu}} \pm 0.35_{\text{syst}}) * 10^{-3}$$

◆ BELLE new result

- Advanced ν Reconstruction with Hadronic Tags

(hep-ex/0311048)

$$|V_{ub}| = (4.66 \pm 0.28_{\text{stat}} \pm 0.19_{\text{exp}} \pm 0.58_{\text{fu}} \pm 0.35_{\text{syst}}) * 10^{-3}$$

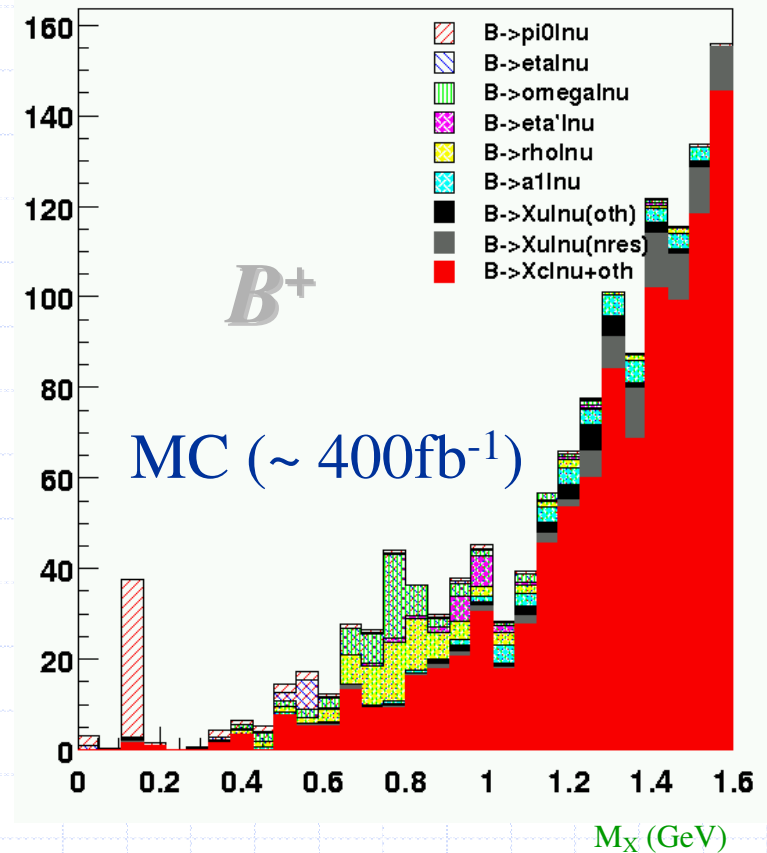


$|V_{ub}|$ from exclusive $B \rightarrow X_u \ell \nu$ channels

◆ Advantages of study of **exclusive decays**

using Recoil Technique:

- Reduced Form Factors dependence.
 - Crossfeed and continuum background highly reduced.
- ## ◆ Event selection and purity can be improved by dedicated cuts for each exclusive channel.
- ## ◆ Events are selected in M_X windows.

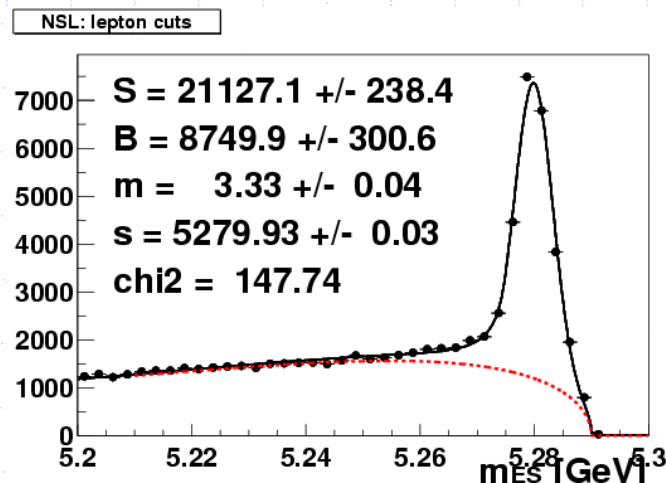


Measurement technique

- ◆ The observed number of events is normalized to the total number of semileptonic decays $B \rightarrow q l \nu$ ($q = u, c$):

$$R_{x/sl} = \frac{\mathcal{B}(B^\pm \rightarrow \pi^0(\rho^0, \omega) l \nu)}{\mathcal{B}(b \rightarrow q l \nu)} = \frac{(N_{excl}^{meas} - BG_{excl}) / \epsilon_{sel}^{excl}}{(N_{sl}^{meas} - BG_{sl})} \times \frac{\epsilon_l^{sl} \epsilon_t^{sl}}{\epsilon_l^{excl} \epsilon_t^{excl}}$$

- ◆ **Additional selection criteria** are imposed to each particular exclusive decay.
- ◆ The number of data events in the M_x signal region, after all analysis cuts, is obtained by an unbinned maximum likelihood **fit to m_{ES}** .



Fit result on data (82 fb⁻¹)

| Parameter | $B^\pm \rightarrow \pi^0 l \nu$ | $B^\pm \rightarrow \rho^0 l \nu$ | $B^\pm \rightarrow \omega l \nu$ |
|--|---------------------------------|----------------------------------|----------------------------------|
| N_{excl}^{meas} | 7.0 ± 2.6 | 12.9 ± 3.6 | 14.5 ± 4.4 |
| BG_{excl} | 0.2 ± 0.2 | 2.5 ± 1.2 | 3.3 ± 1.4 |
| ϵ_{sel}^{excl} | 0.42 ± 0.04 | 0.31 ± 0.03 | 0.20 ± 0.02 |
| $N_{sl}^{meas} - BG_{sl}$ | 19580 ± 230 | 19580 ± 230 | 19580 ± 230 |
| $\frac{\epsilon_l^{sl}}{\epsilon_l^{excl}}$ | 0.92 ± 0.06 | 0.82 ± 0.05 | 0.76 ± 0.04 |
| $\frac{B(b \rightarrow \pi^0(\rho^0, \omega) l \nu)}{B(b \rightarrow q l \nu)} [*10^{-3}]$ | $0.76 \pm 0.30_{stat}$ | $1.41 \pm 0.49_{stat}$ | $2.16 \pm 0.84_{stat}$ |

$$\frac{B(B^\pm \rightarrow \pi^0 l \nu)}{B(B^\pm \rightarrow X l \nu)} = (0.76 \pm 0.30_{stat} \pm 0.07_{MCstat}) 10^{-3}$$

$$\frac{B(B^\pm \rightarrow \rho^0 l \nu)}{B(B^\pm \rightarrow X l \nu)} = (1.41 \pm 0.49_{stat} \pm 0.17_{MCstat}) 10^{-3}$$

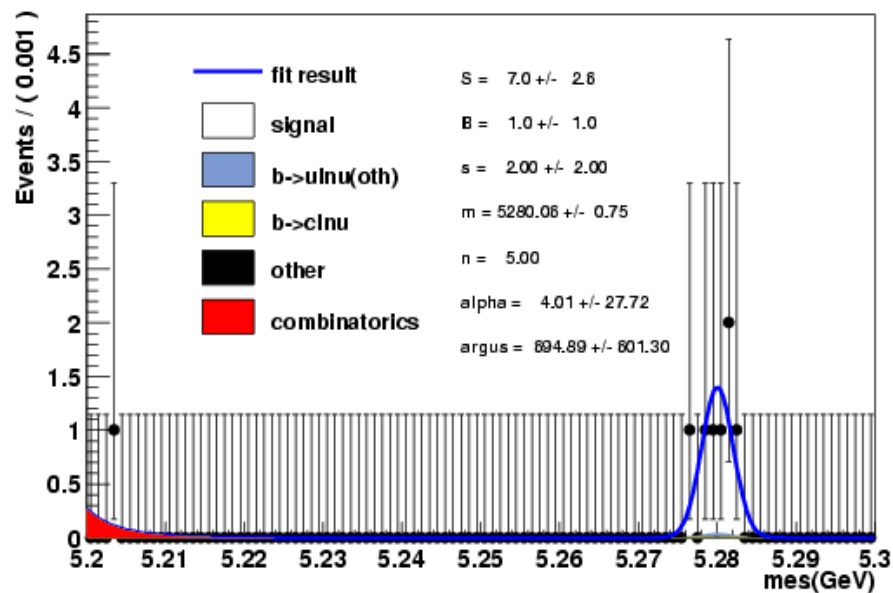
$$\frac{B(B^\pm \rightarrow \omega l \nu)}{B(B^\pm \rightarrow X l \nu)} = (2.16 \pm 0.84_{stat} \pm 0.31_{MCstat}) 10^{-3}$$



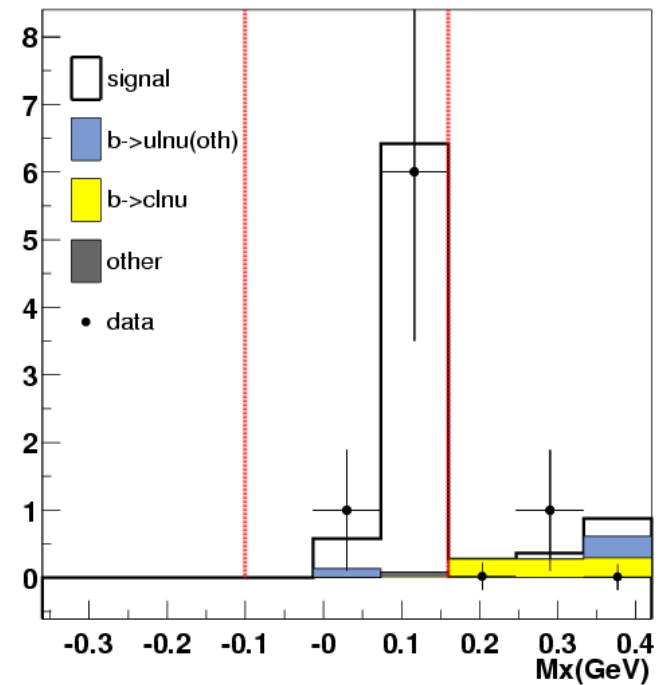
Presented at LP03

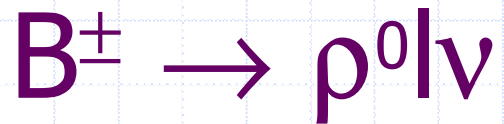
$$BR(B^{\pm} \rightarrow \pi^0 \nu) = (0.78 \pm 0.32_{\text{stat}} \pm 0.13_{\text{syst}}) * 10^{-4}$$

A RooPlot of "mes(GeV)"



data events exclusive

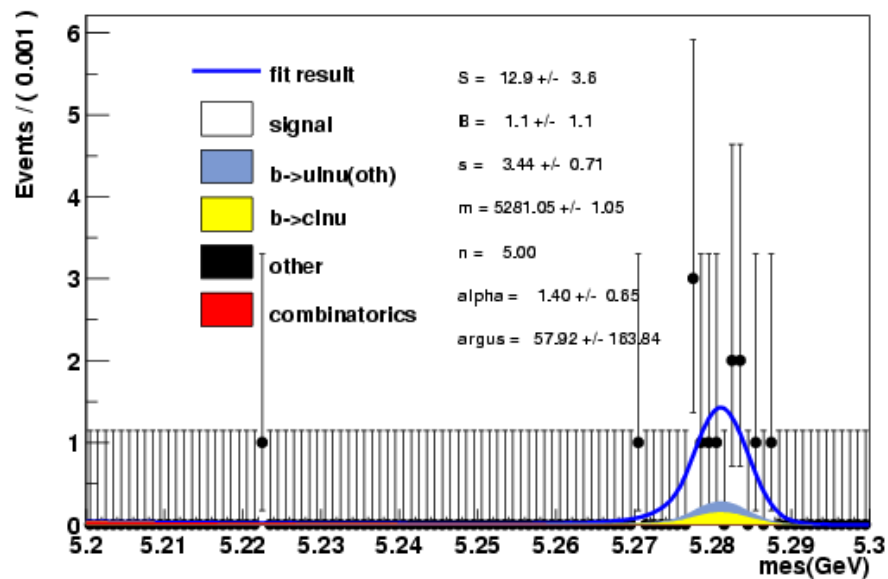




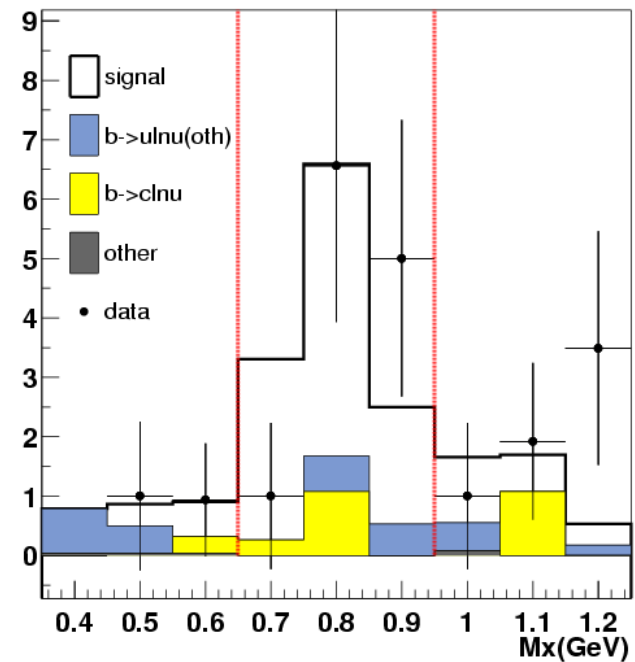
Presented at LP03

$$BR(B^{\pm} \rightarrow \rho^0 l \nu) = (0.99 \pm 0.37_{\text{stat}} \pm 0.19_{\text{syst}}) * 10^{-4}$$

A RooPlot of "mes(GeV)"



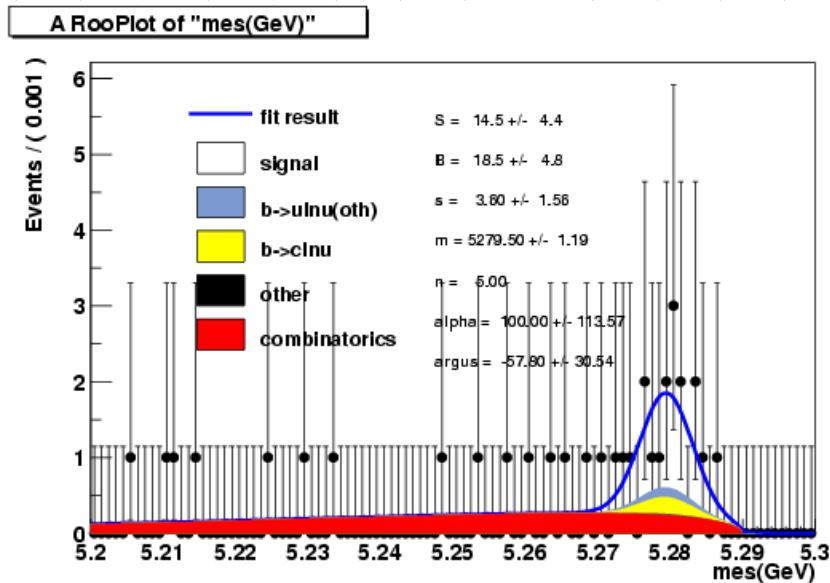
data events exclusive



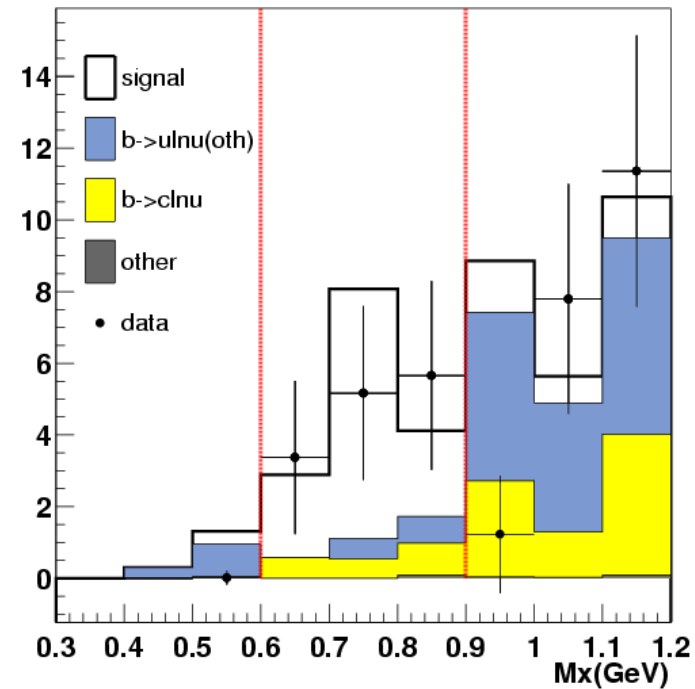
$B^\pm \rightarrow \omega \nu$

Presented at LP03

$$BR(B^\pm \rightarrow \omega \nu) = (2.20 \pm 0.92_{\text{stat}} \pm 0.57_{\text{syst}}) * 10^{-4}$$



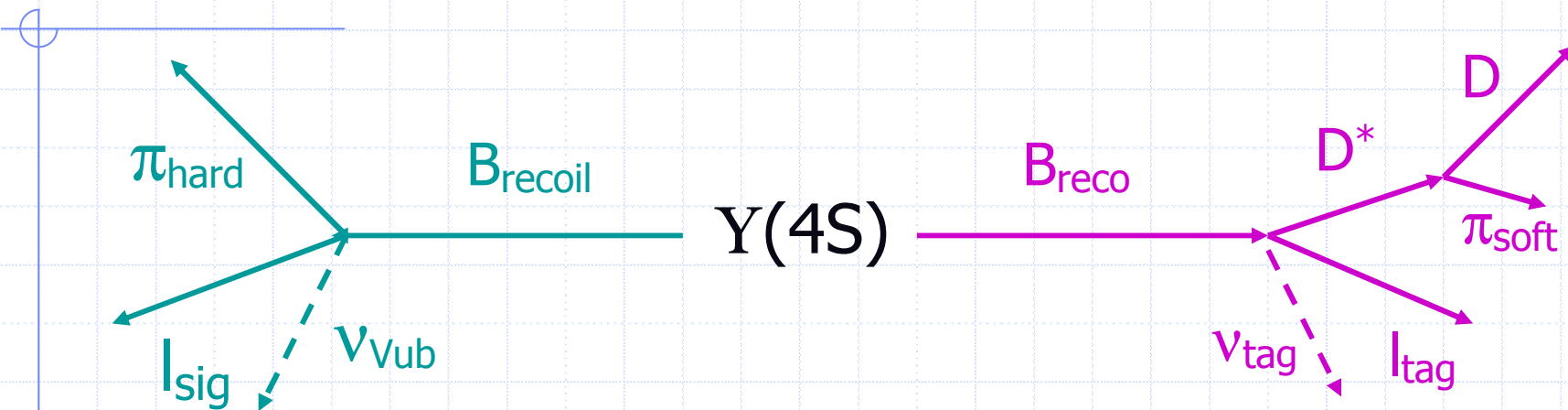
data events exclusive



Charmless Exclusive Branching Fractions

| Decay | BaBar (*10 ⁻⁴) | BELLE (*10 ⁻⁴) | CLEO (*10 ⁻⁴) |
|--|---|--|--|
| $B^0 \rightarrow \pi^- l^+ \nu$ | - | 1.89 ± 0.15 ± 0.30 (2003 - ν Reconstruction) | 1.33 ± 0.18 ± 0.13 (2003 - ν Reconstruction) |
| $B^+ \rightarrow \pi^0 l^+ \nu$ | 0.78 ± 0.32 ± 0.13 (2003 - Recoil) | - | - |
| $B^0 \rightarrow \rho^- l^+ \nu$ | 3.29 ± 0.42 ± 0.79 (2003 - e ⁻ endpoint) | - | 2.17 ± 0.34 ± 0.68 (2003 - ν Reconstruction) |
| $B^+ \rightarrow \rho^0 l^+ \nu$ | 0.99 ± 0.37 ± 0.19 (2003 - Recoil) | 1.44 ± 0.18 ± 0.23 (2002 - ν Reconstruction) | - |
| $B^+ \rightarrow \omega l^+ \nu$ | 2.20 ± 0.92 ± 0.57 (2003 - Recoil) | 1.4 ± 0.4 ± 0.3 (2003 - ν Reconstruction) | - |
| $B^+ \rightarrow \eta l^+ \nu$ | - | - | 0.85 ± 0.31 ± 0.18 (2002 - ν Reconstruction) |
| Other Light Mesons ($\eta', a_0, a_1, b_1, f_0, f_1, h_1, \dots$) | - | - | - |

A new method: Partial Reconstruction



- ◆ Using a double semileptonic decay with partial reconstruction on B_{reco} side can help **improving statistics** without increasing background too much.
- ◆ This technique has been already used in BaBar for $|V_{cb}|$ and B lifetime measurements, using the B_{reco} side as signal side (look @ hep-ex/0308027)
- ◆ B_{reco} Side: $\pi_{\text{soft}} + I_{\text{tag}}$ (partial reconstruction)
- ◆ B_{recoil} Side: $\pi_{\text{hard}} + I_{\text{sig}}$
- ◆ Two unseen neutrinos and no D reconstruction (to improve efficiency).
- ◆ For signal events all remaining tracks come from D decay, for background events further tracks and clusters are expected.

Conclusions

- ◆ Semi-Exclusive reconstruction and recoil technique allowed for a precise inclusive measurement of $|V_{ub}|$.
- ◆ Similar technique used for exclusive semileptonic decays gives:

$$\left\{ \begin{array}{l} \mathcal{B}(B^+ \rightarrow \pi^0 l^+ \nu) = (0.78 \pm 0.32_{stat} \pm 0.13_{syst}) \cdot 10^{-4} \\ \mathcal{B}(B^+ \rightarrow \rho^0 l^+ \nu) = (0.99 \pm 0.37_{stat} \pm 0.19_{syst}) \cdot 10^{-4} \\ \mathcal{B}(B^+ \rightarrow \omega l^+ \nu) = (2.20 \pm 0.92_{stat} \pm 0.57_{syst}) \cdot 10^{-4} \end{array} \right.$$

- Measurements with small number of events but low systematics.
- Increasing luminosity and new theoretical effort can help improving these measurements.
- New techniques (e.g. B_{reco} Partial Reconstruction) also look promising.

Torino Group future tasks



- ◆ Update of $B^+ \rightarrow (\pi^0, \rho^0, \omega) l^+ \nu$ Branching Fractions (with increased luminosity and new theoretical results) expected for summer conferences.
- ◆ Study of missing exclusive channels (B^0 and B^+).
- ◆ Exploitation of alternative approaches to improve signal efficiency.
- ◆ Exclusive measurement of $|V_{ub}|$ (end of 2004?)



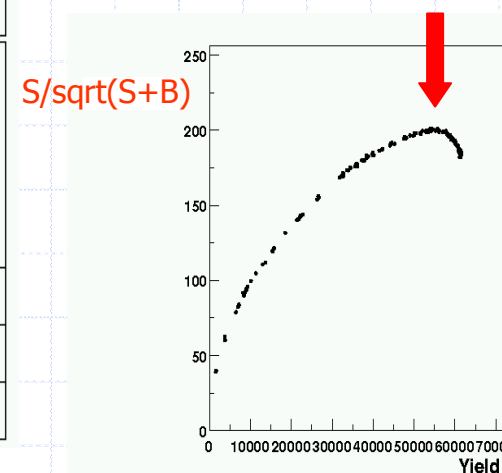
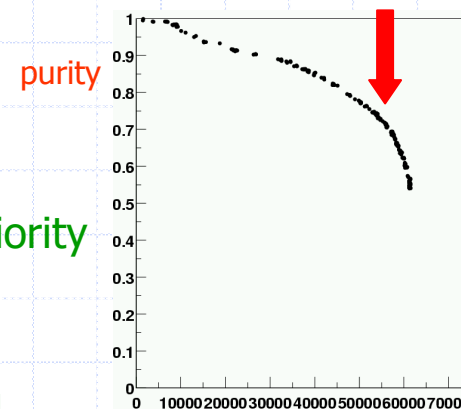
Backup Slides

Selection of B_{reco} candidates

- ◆ The selection of the best B_{reco} relies on:
 - reconstructing all possible $B \rightarrow D(*)X$ decay modes
 - resolving the multiple candidates
 - assigning the candidate to the submode with the highest priority (purity and yields)

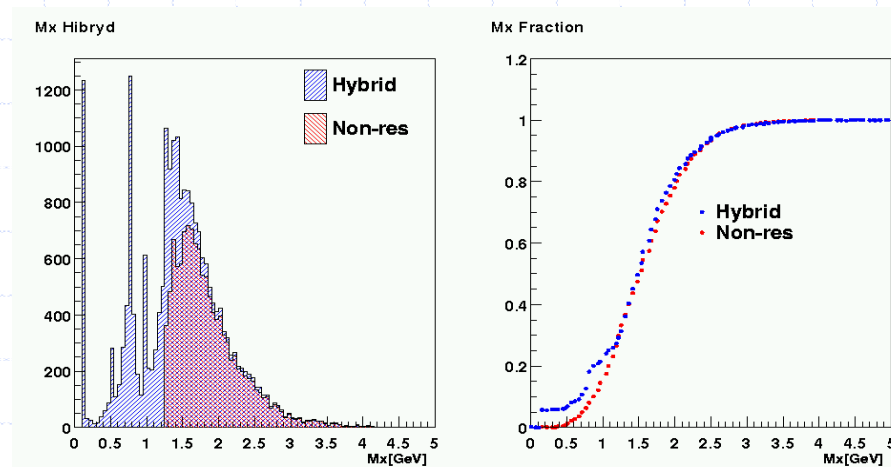
82 fb⁻¹

| Channel | final pur. > 80% | final pur. > 50% | single mode pur. > 10% | final selection (5.4.2) |
|----------------------------|------------------|------------------|------------------------|-------------------------|
| $B^+ \rightarrow D^0 X$ | 19120 ± 170 | 54120 ± 370 | 95204 ± 660 | 100650 ± 640 |
| $B^0 \rightarrow D^+ X$ | 11070 ± 130 | 25720 ± 260 | 55830 ± 480 | 62960 ± 550 |
| $B^+ \rightarrow D^{*0} X$ | 18600 ± 170 | 44270 ± 330 | 75350 ± 580 | 82660 ± 640 |
| $B^0 \rightarrow D^{*+} X$ | 20670 ± 170 | 50300 ± 340 | 55560 ± 390 | 46380 ± 310 |
| Total B^+ | 37720 ± 240 | 98390 ± 500 | 170560 ± 880 | 183310 ± 905 |
| Total B^0 | 31740 ± 210 | 76020 ± 430 | 111390 ± 620 | 109340 ± 630 |
| Total | 69460 ± 320 | 174410 ± 660 | 281950 ± 1080 | 292650 ± 1100 |



Signal MC generation (I)

- ◆ Three kinds of signal MC are used for $B \rightarrow X_u l \nu$:
 - **resonant**: contains **exclusive $B \rightarrow X_u l \nu$ decays** according to measured values and theoretical expectations (ISGW2 model, look @ PRD, 52, 1995 (2783))
 - **non resonant**: the final state hadron is produced with a **continuous invariant mass spectrum** (above $2m_\pi$) and takes into account the **Fermi motion** of the quark b inside the B meson (Neubert and De Fazio, JHEP 9906:17 (1999))
 - **hybrid**: mixes the previous ones in agreement with the measured fraction of resonant and non resonant events below a given **M_x threshold**.

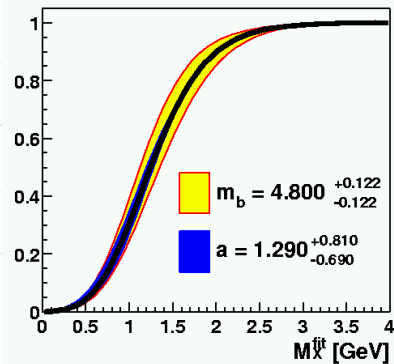
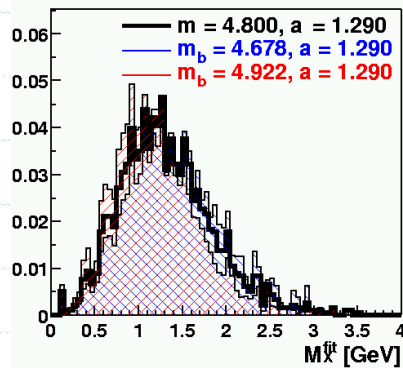


Signal MC generation (II)

| mode | BR | hadron mass [GeV] | mode | BR | hadron mass [GeV] |
|-------------------------------------|----------------------|-------------------|---|----------------------|-------------------|
| $B^0 \rightarrow \pi^- \ell^+ \nu$ | $180 \cdot 10^{-6}$ | 0.13498 | $B^+ \rightarrow \pi^0 \ell^+ \nu$ | $90 \cdot 10^{-6}$ | 0.13957 |
| $B^0 \rightarrow \rho^- \ell^+ \nu$ | $260 \cdot 10^{-6}$ | 0.7685 | $B^+ \rightarrow \eta \ell^+ \nu$ | $30 \cdot 10^{-6}$ | 0.54730 |
| | | | $B^+ \rightarrow \rho^0 \ell^+ \nu$ | $130 \cdot 10^{-6}$ | 0.7685 |
| | | | $B^+ \rightarrow \omega \ell^+ \nu$ | $130 \cdot 10^{-6}$ | 0.78257 |
| $B^0 \rightarrow a_0^- \ell^+ \nu$ | $14 \cdot 10^{-6}$ | 0.9835 | $B^+ \rightarrow \eta' \ell^+ \nu$ | $60 \cdot 10^{-6}$ | 0.95777 |
| $B^0 \rightarrow a_1^- \ell^+ \nu$ | $165 \cdot 10^{-6}$ | 1.23 | $B^+ \rightarrow a_0^0 \ell^+ \nu$ | $7 \cdot 10^{-6}$ | 0.9835 |
| $B^0 \rightarrow a_2^- \ell^+ \nu$ | $14 \cdot 10^{-6}$ | 1.318 | $B^+ \rightarrow a_1^0 \ell^+ \nu$ | $82 \cdot 10^{-6}$ | 1.23 |
| $B^0 \rightarrow b_1^- \ell^+ \nu$ | $102 \cdot 10^{-6}$ | 1.231 | $B^+ \rightarrow a_2^0 \ell^+ \nu$ | $7 \cdot 10^{-6}$ | 1.318 |
| | | | $B^+ \rightarrow b_1^0 \ell^+ \nu$ | $48 \cdot 10^{-6}$ | 1.231 |
| | | | $B^+ \rightarrow f_0^0 \ell^+ \nu$ | $4 \cdot 10^{-6}$ | 1.000 |
| | | | $B^+ \rightarrow f_0^{\prime 0} \ell^+ \nu$ | $4 \cdot 10^{-6}$ | 1.4 |
| | | | $B^+ \rightarrow f_1^0 \ell^+ \nu$ | $41 \cdot 10^{-6}$ | 1.2822 |
| | | | $B^+ \rightarrow f_1^{\prime 0} \ell^+ \nu$ | $41 \cdot 10^{-6}$ | 1.4268 |
| | | | $B^+ \rightarrow f_2^0 \ell^+ \nu$ | $4 \cdot 10^{-6}$ | 1.275 |
| | | | $B^+ \rightarrow f_2^{\prime 0} \ell^+ \nu$ | $4 \cdot 10^{-6}$ | 1.525 |
| | | | $B^+ \rightarrow h_1^0 \ell^+ \nu$ | $24 \cdot 10^{-6}$ | 1.17 |
| | | | $B^+ \rightarrow h_1^{\prime 0} \ell^+ \nu$ | $24 \cdot 10^{-6}$ | 1.40 |
| exclusive | $735 \cdot 10^{-6}$ | | exclusive | $730 \cdot 10^{-6}$ | |
| inclusive | $616 \cdot 10^{-6}$ | | inclusive | $616 \cdot 10^{-6}$ | |
| total | $1351 \cdot 10^{-6}$ | | total | $1346 \cdot 10^{-6}$ | |

Systematic uncertainties

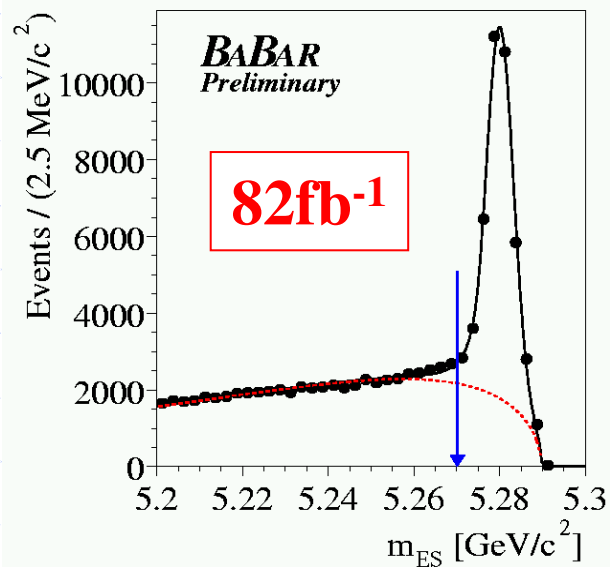
- ◆ The Fermi motion of the b quark inside the b meson affects the M_X distribution and the efficiency of the M_X cut.



| Source | $\Delta R_{u/sl} / R_{u/sl} [\%]$ |
|---|-----------------------------------|
| Data statistics | 12.7 |
| MC statistics | 4.5 |
| Electron identification | 1.0 |
| Muon identification | 1.0 |
| K^\pm identification | 2.3 |
| Tracking efficiency | 1.0 |
| Photon resolution | 4.7 |
| K_L interactions | 1.0 |
| B_{reco} composition, background subtraction | 3.8 |
| Binning effects | 1.2 |
| $\varepsilon_t^{sl} / \varepsilon_t^{ul}$ | 3.0 |
| Detector systematic error | 8.7 |
| $B \rightarrow D^{(*,**)} \ell \bar{\nu} X$ branching fractions | 4.0 |
| D branching fractions | 1.8 |
| Modeling of $B \rightarrow X_c \ell \bar{\nu}$ and $X_c \rightarrow Y \ell \bar{\nu}$ | 4.4 |
| Excl. $b \rightarrow u \ell \bar{\nu}$ branching fractions | 2.7 |
| Incl. $b \rightarrow u \ell \bar{\nu}$ branching fractions | 0.8 |
| Hadronization error | 3.0 |
| $s\bar{s}$ popping | 3.7 |
| Modeling of $B \rightarrow X_u \ell \bar{\nu}$ | 5.5 |
| m_b dependence | 16.0 ^a |
| λ_1 dependence | 6.0 |
| Total theoretical error | 17.5 |

Expected yields from MC

- ◆ Same technique of inclusive analysis.
- ◆ Fitted hadronic mass and charged tracks multiplicity are used to separate resonances.
- ◆ Using MC estimation, ~ 170 $B \rightarrow X_u l \nu$ events are expected in 82 fb^{-1} of data after all cuts, for $M_X < 1.55 \text{ GeV}$.



$N_{SL} = 32K$ $B \rightarrow X l \nu$ events in data (20.5K B^+ , 11.5K B^0)

$$N_{B \rightarrow \pi^0(\rho, \omega) l \nu} \simeq N_{sl} \frac{\mathcal{B}(B \rightarrow \pi^0(\rho, \omega) l \nu)}{\mathcal{B}(B^\pm \rightarrow X l \nu)} \simeq 20K \frac{\mathcal{B}(B \rightarrow \pi^0(\rho, \omega) l \nu)}{0.102}$$

17 $B^+ \rightarrow \pi^0 l \nu$

19 $B^0 \rightarrow \pi^+ l \nu$

25 $B^+ \rightarrow \rho^0 l \nu$

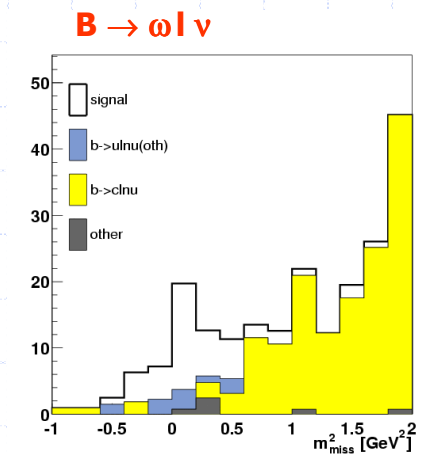
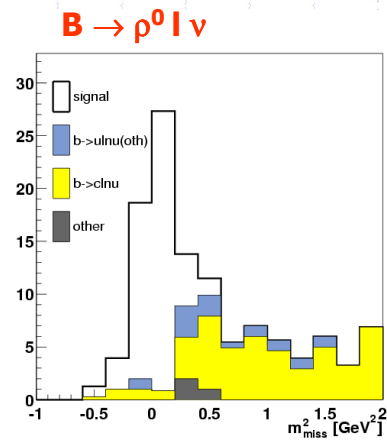
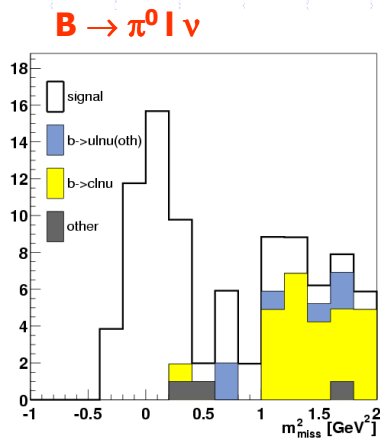
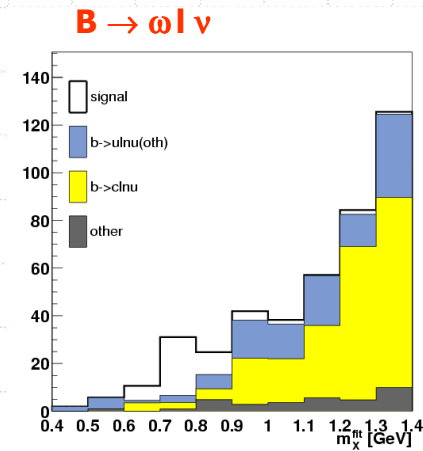
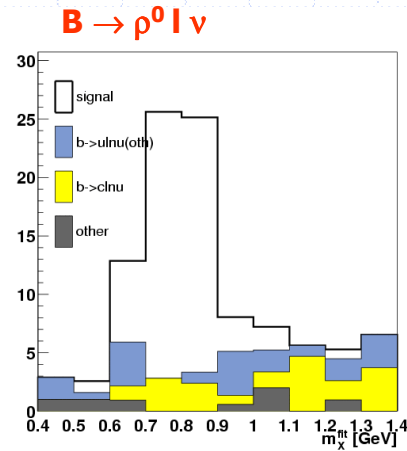
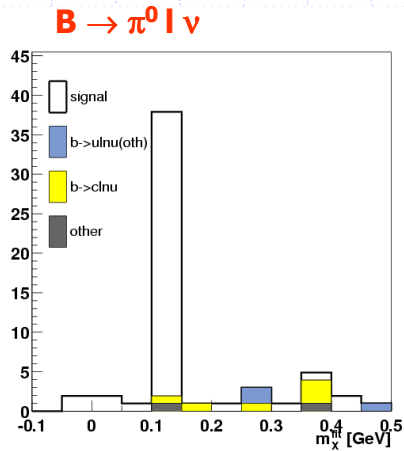
27 $B^0 \rightarrow \rho^+ l \nu$

25 $B^+ \rightarrow \omega l \nu$

17 $B^0 \rightarrow a_1 l \nu$

15 $B^+ \rightarrow a_1 l \nu$

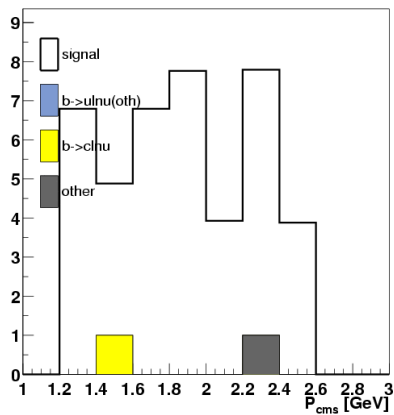
M_x & M_{miss}^2 for $B^\pm \rightarrow (\pi^0, \rho^0, \omega) l \nu$



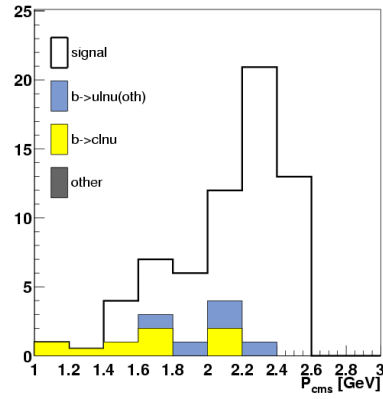
MC
~240 fb⁻¹

p_l^* & N_{tracks} for $B^\pm \rightarrow (\pi^0, \rho^0, \omega) l \nu$

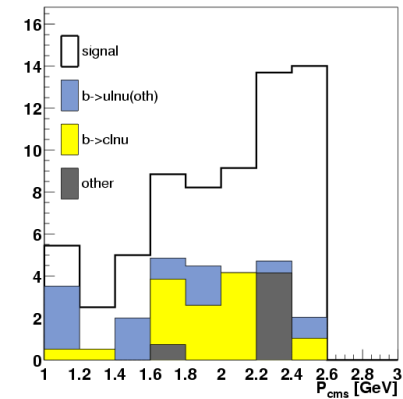
$B \rightarrow \pi^0 l \nu$



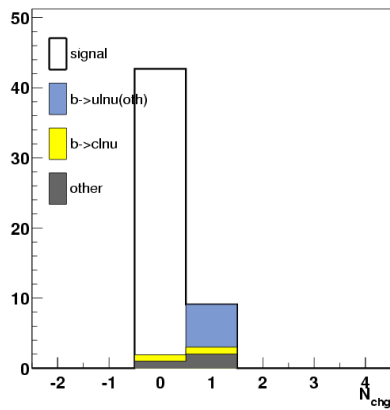
$B \rightarrow \rho^0 l \nu$



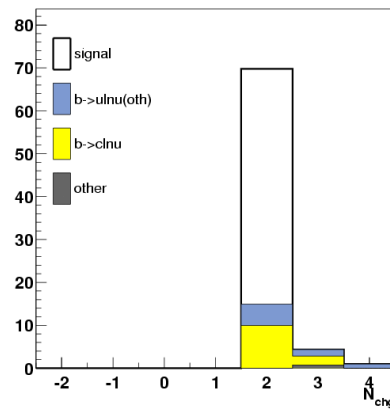
$B \rightarrow \omega l \nu$



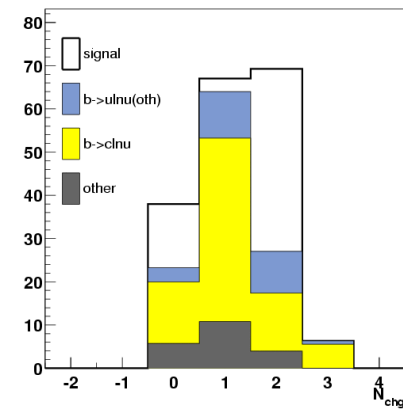
$B \rightarrow \pi^0 l \nu$



$B \rightarrow \rho^0 l \nu$



$B \rightarrow \omega l \nu$



MC
~240 fb⁻¹

Event selection

- ◆ Selection cuts are optimized in order to maximize statistical significance:

| Selection Criteria | $B \rightarrow \pi^0 l \nu$ | $B \rightarrow \rho^0 l \nu$ | $B \rightarrow \omega l \nu$ | $B \rightarrow q l \nu$ |
|-------------------------------------|----------------------------------|------------------------------------|------------------------------------|-------------------------|
| B_{reco} candidate | purity cuts | purity cuts | purity cuts | purity cuts |
| Min. lept. momentum | $p^* > 1.0 \text{ GeV}$ | $p^* > 1.0 \text{ GeV}$ | $p^* > 1.0 \text{ GeV}$ | $p^* > 1.0 \text{ GeV}$ |
| Number of leptons | $N_{lepton} = 1$ | $N_{lepton} = 1$ | $N_{lepton} = 1$ | $N_{lepton} > 0$ |
| Lept. Charge - B Flav. | $Q_{b(recoil)} Q_l > 0$ | $Q_{b(recoil)} Q_l > 0$ | $Q_{b(recoil)} Q_l > 0$ | $Q_{b(recoil)} Q_l > 0$ |
| Total charge | $Q_{tot} = 0$ | $Q_{tot} = 0$ | $Q_{tot} = 0$ | - |
| Missing mass sq. | $M_{miss}^2 < 0.4 \text{ GeV}^2$ | $M_{miss}^2 < 0.3 \text{ GeV}^2$ | $M_{miss}^2 < 0.6 \text{ GeV}^2$ | - |
| Kaon Veto | $N_{K^\pm} + N_{K_S} = 0$ | $N_{K^\pm} + N_{K_S} = 0$ | $N_{K^\pm} + N_{K_S} = 0$ | - |
| N charged tracks | $N_{chg} = 0$ | $N_{chg} = 2$ | $N_{chg} = 2$ | - |
| $m_X \text{ fit} - m_X \text{ chg}$ | - | $\Delta M_{chg} < 0.1 \text{ GeV}$ | $\Delta M_{chg} > 0.1 \text{ GeV}$ | - |
| Lower m_X Cut | $m_X > -0.1 \text{ GeV}$ | $m_X > 0.65 \text{ GeV}$ | $m_X > 0.6 \text{ GeV}$ | - |
| Upper m_X Cut | $m_X < 0.16 \text{ GeV}$ | $m_X < 0.95 \text{ GeV}$ | $m_X < 0.9 \text{ GeV}$ | - |

- ◆ " ρ^0 " is defined as $\pi^+\pi^-$ in the mass window $0.65 < m_{\pi^+\pi^-} < 0.95 \text{ GeV}$

Sistematic uncertainties

| | Relative Uncertainty on $R_{x/sl}(\%)$ | | |
|---------------------------------------|--|---|----------------------------------|
| | $B^\pm \rightarrow \pi^0 l \nu$ | $B^\pm \rightarrow \text{“}\rho^0\text{” } l \nu$ | $B^\pm \rightarrow \omega l \nu$ |
| electron id | 1.3 | 4.0 | 2.5 |
| muon id | 0.5 | 1.3 | 0.3 |
| K^\pm id | 0.0 | 0.3 | 3.0 |
| tracking efficiency | 0.8 | 4.8 | 4.4 |
| photon resolution | 7.5 | 5.2 | 4.1 |
| m_{ES} fit | 8.5 | 11.0 | 3.7 |
| cross-feed $B^0 \rightarrow B^+$ | 1.5 | 1.8 | 2.4 |
| $\epsilon_t^{sl} / \epsilon_t^u$ | 8.0 | 8.0 | 8.0 |
| lepton momentum cut | 2.0 | 4.0 | 4.0 |
| $B \rightarrow D l \nu X$ and D BRs | 0.0 | 1.0 | 1.4 |
| $b \rightarrow u l \nu$ resonant | 0.5 | 3.2 | 5.8 |
| $b \rightarrow u l \nu$ non-resonant | 0.5 | 6.8 | 16.4 |
| Total error | 14.2 | 17.1 | 24.5 |