## **Open charm mesons measurement** in ALICE

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## **Physics motivation**

## **Charm production: pp collisions**

- Hard partonic processes (q-qbar annihilation, gluon fusion)
  - pQCD phenomenon taking place on short time-scale ( $\approx 1/m_Q$ )



## **Charm production: AA collisions**

- Hard primary production in parton processes (pQCD)
  - Binary scaling for hard process yield:

$$\mathrm{d}N_{AA} / \mathrm{d}p_T = N_{coll} \times \mathrm{d}N_{pp} / \mathrm{d}p_T$$

- long lifetime of charm quarks allows them to live through the thermalization phase of the QGP and be affected by its presence
- Secondary (thermal) c-cbar production in the QGP
  - m<sub>c</sub> (≈1.2 GeV) only 10%-50% higher than predicted temperature of QGP at the LHC (500-800 MeV)
  - Thermal yield expected much smaller than hard primary production

✓ can be observed if the pQCD production in A-A is precisely understood

## **Binary scaling break-up**



#### ✓ Anti-shadowing and shadowing

- k<sub>T</sub> broadening (Cronin effect)
- Parton saturation (Color Glass Condensate)

Present also in pA (dA) collisions Concentrated at lower  $p_T$ 



- Energy loss
  - ✓ Mainly by gluon radiation
- In medium hadronization
  - ✓ *Recombination vs. fragmentation*

Only in AA collisions Dominant at higher  $p_{\tau}$ 





## Final state effects: energy loss

BDMPS formalism for radiative energy loss

Baier et al., Nucl. Phys. B483 (1997) 291)

average energy loss

Casimir coupling factor

distance travelled in the medium

transport coefficient of the medium

 $\alpha_{s} C_{R} q L^{2}$ 

- Energy loss for heavy flavours is expected to be reduced by:
  - Casimir factor
    - *ight hadrons originate predominantly from gluon jets, heavy flavoured hadrons originate from heavy quark jets*
    - $\checkmark$  C<sub>R</sub> is 4/3 for quark-gluon coupling, 3 for gluon-gluon coupling
  - Dead-cone effect
    - ✓ gluon radiation expected to be suppressed for  $\theta < M_{Q}/E_{Q}$ 
      - Dokshitzer & Karzeev, Phys. Lett. **B519** (2001) 199
      - <sup>[]</sup> Armesto et al., Phys. Rev. D69 (2004) 114003

## **Experimental observables**



Nuclear modification factor

$$R_{AA}(p_T) = \frac{1}{\langle N_{coll} \rangle} \frac{dN_{AA} / dp_T}{dN_{pp} / dp_T}$$

•  $R_{AA} \neq 1 \Rightarrow$  binary scaling violation

✓ Low p<sub>T</sub> → main effect = nuclear shadowing
 ✓ High p<sub>T</sub> → main effect = energy loss



## **RHIC results: non-photonic electrons**

#### Nuclear modification factor



## **Charm in ALICE**

## Charm at the LHC (I)

	SPS	RHIC	LHC
√s (GeV)	17.2	200	5500
N <sub>cc</sub>	≈ 0.2	≈10	≈100-200
x (at y=0)	≈ 10-1	≈ 10-2	≈ 10-4

#### Large cross-section

Much more abundant production with respect to SPS and RHIC

$$\sigma_{LHC}^{c\bar{c}} \approx 10 - 20 \times \sigma_{RHIC}^{c\bar{c}}$$

#### Small x

$$x_{1} = \frac{A_{1}}{Z_{1}} \frac{M_{c\bar{c}}}{\sqrt{s_{pp}}} e^{y_{c\bar{c}}} \qquad x_{2} = \frac{A_{2}}{Z_{2}} \frac{M_{c\bar{c}}}{\sqrt{s_{pp}}} e^{-y_{c\bar{c}}}$$

- unexplored small-x region can be probed with charm at low  $p_{\rm T}$  and/or forward rapidity
  - ✓ down to  $x\sim 10^{-4}$  at y=0 and  $x\sim 10^{-6}$  in the muon arm



## Charm at the LHC (II)

- p-p collisions
  - Test of pQCD in a new energy and x regime
  - Reference for Pb-Pb (necessary for  $R_{AA}$ )
- p-Pb collisions
  - Probe nuclear PDFs at LHC energy
  - Disentangle initial and final state effects
- Pb-Pb collisions
  - Probe the medium formed in the collision
- WARNING: pp, pPb and PbPb will have different √s values
  - Need to extrapolate from 14 TeV to 5.5 TeV to compute R<sub>AA</sub>

✓ Small (≈ 10%) theoretical uncertainty on the ratio of results at 14 and 5.5 TeV



## **Charmed mesons and baryons**

- Weakly decaying charm states
  - Mean proper length  $\approx$  100  $\mu m$
- Main selection tool: displacedvertex
  - Tracks from open charm decays are typically displaced from primary vertex by ≈100 µm
  - Need for high precision vertex detector (resolution on track impact parameter ≈ tens of microns)

Meson	Mass (MeV)	cτ (μm)
$D^+(c\overline{d})$	1869	312
$D^0(c\overline{u})$	1865	123
$D_s^+(c\overline{s})$	1968	147
$\Lambda_{c}^{+}(udc)$	2285	60
$\Xi_c^+(usc)$	2466	132
$\Xi_c^0(dsc)$	2472	34
$\Omega_c^0(ssc)$	2698	21





## **Heavy-flavours in ALICE**

#### ALICE channels:

- electronic (|η|<0.9)</li>
- muonic (-4<η<-2.5)</li>
- hadronic (|η|<0.9)</li>

#### ALICE coverage:

- $low-p_T$  region
- central and forward rapidity regions
- Precise vertexing in the central region to identify D ( $c\tau \sim 100-300 \mu$ m) and B ( $c\tau \sim 500 \mu$ m) decays





#### **Time Projection Chamber and Time Of Flight**

- TPC Provides:
  - Many 3D points per track
  - Tracking efficiency > 90%
  - + Particle identification by dE/dx
    - ✓ in the low-momentum region
      ✓ in the relativistic rise





• TOF Provides:

pion, Kaon identification (with contamination <10%) in the momentum range 0.2-2.5 GeV/c

proton identification (with contamination <10%) in the momentum range 0.4-4.5 GeV/c

## D mesons simulation and reconstruction

## **D** mesons: hadronic decays

Most promising channels for exclusive charmed meson reconstruction

Meson	Final state	# charged bodies	Branching Ratio	
	$\rightarrow$ K <sup>-</sup> $\pi$ <sup>+</sup>	2 3.8%		
Do			Total	7.48%
	$\rightarrow$ K <sup>-</sup> $\pi^+\pi^+\pi^-$	4	Non resonant	1.74%
			$D^{0} \rightarrow K^{-}\pi^{+}\rho^{0} \rightarrow K^{-}\pi^{+}\pi^{-}$	6.2%
D⁺	$\rightarrow K^{-}\pi^{+}\pi^{+}$	3	Total	9.2%
			Non resonant	8.8%
			$D^+ \rightarrow Kbar^{0*}(892)\pi^+ \rightarrow K^-\pi^+\pi^+$	1.29%
			$D^* \rightarrow Kbar^{0*}$ (1430) $\pi^+ \rightarrow K^- \pi^+ \pi^+$	2.33%
			Total	4.3%
$D_{s}^{+}$	$\rightarrow K^+K^-\pi^+$	3	$D_{s}^{+} \rightarrow K^{+}Kbar^{0*} \rightarrow K^{+}K^{-}\pi^{+}$	2.0%
			$D_{s}^{+} \rightarrow \phi \pi^{+} \rightarrow K^{+} K^{-} \pi^{+}$	1.8%

## D mesons in central barrel

- No dedicated trigger in the central barrel → extract the signal from Minimum Bias events
  - Large combinatorial background (benchmark study with dN<sub>ch</sub>/dy = 6000 in central Pb-Pb!)
- SELECTION STRATEGY: invariant-mass analysis of fullyreconstructed topologies originating from displaced vertices
  - build pairs/triplets/quadruplets of tracks with correct combination of charge signs and large impact parameters
  - particle identification to tag the decay products
  - calculate the vertex (DCA point) of the tracks
  - good pointing of reconstructed D momentum to the primary vertex



#### $D^0 \rightarrow K^-\pi^+$ : selection of candidates









With  $dN_{ch}/dy = 3000$  in Pb-Pb, S/B larger by  $\times 4$ and significance larger by  $\times 2$ 

#### Motivation to study other mesons (D<sub>s</sub> & D<sup>+</sup>)

- To measure charm yield more precisely we need to measure as many channels as we can
- Study of different ways of hadronization:
  - String fragmentation:
     D<sub>s</sub><sup>+</sup> (cs) / D<sup>+</sup> (cd) ~ 1/3
  - Recombination:

 $D_{s^{+}}(cs) / D^{+}(cd) \sim N(s)/N(d) (\sim 1 \text{ at LHC?})$ 

 $D^+ \rightarrow K^-\pi^+\pi^+\nu s$ ,  $D^0 \rightarrow K^-\pi^+$ 

#### Advantages

- $D^{\star}$  has a longer mean proper length (ct ~312  $\mu$ m compared to ~123 mm of the  $D^{o}$ )
- $D^+ \rightarrow K^- \pi^+ \pi^+$  has a larger branching ratio (9.2% compared to 3.8% for  $D^0 \rightarrow K^- \pi^+$ )
- Possibility to exploit the resonant decay through Kbar<sup>0\*</sup> to enhance S/B

#### Drawbacks

- Larger combinatorial background (3 decay products instead of the 2 of the  $D^o \rightarrow K^-\pi^+$ )
- Smaller  $\langle p_T \rangle$  of the decay products (~ 0.7 GeV/c compared to ~ 1 GeV/c of the D<sup>o</sup> decay products)
- D<sup>+</sup> less abundant than D<sup>0</sup> (factor 2-3)

## **D**<sup>+</sup> final selection steps (I)

- Four selection variables:
  - Distance between primary and secondary vertex (d<sub>PS</sub>)
  - cosθ<sub>point</sub>
  - Sum of squared impact parameters  $s = d_{01}^{2} + d_{02}^{2} + d_{03}^{2}$
  - Max. p<sub>T</sub> among the 3 tracks
     p<sub>M</sub>=Max{p<sub>T1</sub>,p<sub>T2</sub>,p<sub>T3</sub>}





## **D**<sup>+</sup> **Results: PbPb** (I)

- Significance and relative statistical error vs.  $D^{\scriptscriptstyle +}$   $p_{\scriptscriptstyle T}$ 
  - S/ev~10⁻³, B/ev ~10⁻⁴
  - Significance and relative statistical error (=1/ $\!\sqrt{}$ S) normalized to 107 central PbPb events



## D<sup>+</sup> Results: pp (I)

- Significance and relative statistical error vs.  $D^{\scriptscriptstyle +} \, p_{\scriptscriptstyle T}$ 
  - S/ev~5 10⁻⁶, B/ev ~5 10⁻⁶
  - Significance and relative statistical error (=1/ $\!\!\sqrt{}$ S) normalized to 10° pp Minimum Bias events



 $D_{c}^{+} \rightarrow K^{+}K^{-}\pi^{+} \quad vs. \ D^{+} \rightarrow K^{-}\pi^{+}\pi^{+}$ 

#### Advantages

- Smaller combinatorial background if particle identification is efficient (kaons are less abundant than pions)
- Larger fraction of  $D_{s^+} \rightarrow K^+ K^- \pi^+$  from resonant decays (through KbarO\* or  $\phi$ ) with respect to D<sup>+</sup>

#### Drawbacks

 $D_{s}^{+}$  has a smaller mean proper length (ct =147  $\mu m$  compared to 312  $\mu m$  of the D^+)

D<sub>s</sub><sup>+</sup> → K<sup>+</sup>K<sup>-</sup> $\pi$ <sup>+</sup> has a smaller Branching Ratio (4.3%) with respect to D<sup>+</sup> → K<sup>-</sup> $\pi$ <sup>+</sup> $\pi$ <sup>+</sup> (BR=9.2%)

### **D**<sub>s</sub>: Resonances channels separation

- Calculation of the invariant mass of the KK and Kπ pairs
- Comparing them to m(φ) and m(KO\*)



0



#### **D<sub>s</sub>: Final triplet multicut** (under development)

#### • 4 variables

- Cosine of pointing angle
- Cosine of opening angle
- Sum of impact parameters squared
- Distance between primary and secondary vertex





## **Perspective for D<sup>o</sup> D<sup>+</sup> energy loss**

 $D^{0} \rightarrow K^{-}\pi^{+} : R_{AA}$ 

- 1 year at nominal luminosity
  - 1 month  $\rightarrow$  10<sup>7</sup> central Pb-Pb events
  - 10 months  $\rightarrow$  10<sup>9</sup> pp events

$$R_{AA}^{D}(p_{t}) = \frac{1}{\langle N_{coll} \rangle} \frac{dN_{AA}^{D} / dp_{t}}{dN_{pp}^{D} / dp_{t}}$$





- Statistical error bars from 10<sup>9</sup> pp Min. Bias events and 10<sup>7</sup> central PbPb events (1 year of data taking)
  - Statistical error smaller than the syst. errors up to 10 GeV/c







Mass (GeV/ $c^2$ )

- Pseudorapidity coverage:
- Azimuthal coverage: •

#### Provides:

Rin

 $\mathsf{R}_{\mathsf{ext}}$ 

- pion, Kaon identification (with contamination) <10%) in the momentum range 0.2-2.5 GeV/c
- proton identification (with contamination <10%)  $_{-2.5}$ in the momentum range 0.4-4.5 GeV/c

## **Charm production at the LHC**

- ALICE baseline for charm cross-section and  $p_{\tau}$  spectra:
  - NLO pQCD calculations (Mangano, Nason, Ridolfi, NPB373 (1992) 295.)

 $\checkmark$  Theoretical uncertainty = factor 2-3

- Average between cross-sections obtained with MRSTHO and CTEQ5M sets of PDF
  - $\checkmark \approx 20\%$  difference in  $\sigma_{\rm cc}$  between MRST HO and CTEQ5M
- Binary scaling + shadowing (EKS98) to extrapolate to p-Pb and Pb-Pb

	Pb-Pb	p-Pb	
System	(0-5% centr.)	(min. bias)	<i>pp</i>
√ <i>s</i> <sub>NN</sub>	5.5 TeV	8.8 TeV	14 TeV
σ <sup>cc</sup> <sub>NN</sub> w/o shadowing	6.64 mb	8.80 mb	11.2 mb
C <sub>shadowing</sub> (EKS98)	0.65	0.80	1.
$\sigma^{cc}_{NN}$ with shadowing	4.32 mb	7.16 mb	11.2 mb
N <sup>cc</sup> tot	115	0.78	0.16
D°+D°bar	141	0.93	0.19
D⁺+D⁻	45	0.29	0.06
$D_{s}^+ + D_{s}^-$	27	0.18	0.04
$\Lambda_{c}^{+}+\Lambda_{c}^{-}$	18	0.12	0.02

## $D^{0} \rightarrow K^{-}\pi^{+}$ : heavy-to-light ratios

#### I year at nominal luminosity

- 1 month  $\rightarrow$  10<sup>7</sup> central Pb-Pb events
- 10 months  $\rightarrow$  10<sup>9</sup> pp events

 $R_{D/h}(p_t) = R_{AA}^D(p_t)/R_{AA}^h(p_t)$ 



## **Perspective for D**<sup>+</sup> $v_2$

## **Motivation and method**

- GOAL: Evaluate the statistical error bars for measurements of  $v_2$  for D<sup>±</sup> mesons decaying in  $K\pi\pi$ 
  - $v_2$  vs. centrality ( $p_T$  integrated)
  - $v_2$  vs.  $p_T$  in different centrality bins
- TOOL: fast simulation (ROOT + 3 classes + 1 macro)
  - Assume to have only signal
  - Generate  $N^{D_{\pm}}(\Delta b, \Delta p_{\tau})$  events with 1 D<sup>±</sup> per event
  - For each event
    - □ Generate a random reaction plane
    - □ Get an event plane (with correct event plane resolution)
    - □ Generate the  $D^+$  azimuthal angle ( $\varphi^D$ ) according to the probability distribution  $p(\varphi) \propto 1 + 2v_2 \cos \left[2(\varphi - \Psi_{RP})\right]$
    - **Since** Since  $\varphi^{D}$  with the experimental resolution on  $D^{\pm}$  azimuthal angle
    - $\Box$  Calculate  $v'_2(D^+)$ , event plane resolution and  $v_2(D^+)$

## **D**<sup>±</sup> statistics

b <sub>min</sub> -b <sub>max</sub> (fm)	σ (%)	N <sub>events</sub> (10 <sup>6</sup> )	N <sub>cc</sub> / ev.	D <sup>±</sup> yield/ev.
0-3	3.6	0.72	118	45.8
3-6	11	2.2	82	31.8
6-9	18	3.6	42	16.3
9-12	25.4	5.1	12.5	4.85
12-18	42	8.4	1.2	0.47



- $N_{events}$  for 2.107 MB triggers
- N<sub>cc</sub> = number of c-cbar pairs
  - MNR + EKS98 shadowing
  - Shadowing centrality dependence from Emelyakov et al., PRC 61, 044904
- D<sup>±</sup> yield calculated from N<sub>cc</sub>
  - Fraction N<sup>D±</sup>/N<sub>cc</sub> (≈0.38) from tab. 6.7 in chapt. 6.5 of PPR
  - Geometrical acceptance and reconstruction efficiency
    - Extracted from 1 event with 20000 D<sup>±</sup> in full phase space
  - B. R.  $D^{\pm} \rightarrow K\pi\pi = 9.2$  %

#### Selection efficiency

- No final analysis yet
- $1 = 1 = 1 = 0 \quad (a = 0 = 0)$

## **Event plane resolution scenario**

• Event plane resolution depends on  $v_2$  and multiplicity



## **Results:** v<sub>2</sub> vs. centrality



- Would be larger in a scenario with worse event plane resolution
- May prevent to draw conclusions in case of small anisotropy of D mesons

**Results:**  $v_2$  vs.  $p_T$ 

2.107 MB events



## Worse resolution scenario

Low multiplicity and low v2





• Huge number ( $\approx 10^{10}$ ) of combinatorial K $\pi\pi$  triplets in a central event

•  $\approx 10^8$  triplets in invariant mass range 1.84 (M(1.90 GeV/c<sup>2</sup>)) (D<sup>±</sup> peak ± 3 $\sigma$ )

✓ Final selection cuts not yet ready

- Signal almost free from background only for p<sub>T</sub>>5-6 GeV/c
- Need to separate signal from background in v<sub>2</sub> calculation
- FIRST IDEA: sample candidate  $K\pi\pi$  triplets in bins of azimuthal angle relative to the event plane ( $\Delta \varphi = \varphi \Psi_2$ )
  - Build invariant mass spectra in bins of  $\Delta \phi$  and centrality /  $p_{\tau}$



Analysis in bins of  $\Delta \varphi$  (II)

• Fit number of D<sup>±</sup> vs.  $\Delta \phi$  with A[1 + 2v<sub>2</sub>cos(2 $\Delta \phi$ )]



## **Other ideas for background**

#### Different analysis methods to provide:

- Cross checks
- Evaluation of systematics
- Apply the analysis method devised for  $\Lambda s$  by Borghini and Ollitrault [ PRC 70 (2004) 064905 ]

 $N_{\text{pairs}}(M) = N_b(M) + N_{\Lambda}(M). \longrightarrow N_{\text{pairs}}(M)v_{c,n}(M) = N_b(M)v_{c,n}^{(b)}(M) + N_{\Lambda}(M)v_{c,n}^{\Lambda},$  $N_{\text{pairs}}(M)v_{s,n}(M) = N_b(M)v_{s,n}^{(b)}(M) + N_{\Lambda}(M)v_{s,n}^{\Lambda}.$ 

- To be extended from pairs (2 decay products) to triplets (3 decay products)
- Extract the cos[2( $\varphi$ - $\Psi_{RP}$ )] distribution of combinatorial K $\pi\pi$  triplets from:
  - Invariant mass side-bands
  - Different sign combinations (e.g.  $K^{\dagger}\pi^{\dagger}\pi^{\dagger}$  and  $K^{-}\pi^{-}\pi^{-}$ )

## **Conclusions on v<sub>2</sub>**

- Large stat. errors on  $v_2$  of  $D^{\pm} \rightarrow K\pi\pi$  in 2.107 MB events
- How to increase the statistics?
  - Sum  $D^0 \rightarrow K\pi$  and  $D^{\pm} \rightarrow K\pi\pi$ 
    - ✓ Number of events roughly  $\times 2 \rightarrow$  error bars on  $v_2$  roughly  $/ \sqrt{2}$
    - ✓ Sufficient for  $v_2$  vs. centrality ( $p_T$  integrated)
  - Semi-peripheral trigger
    - $\checkmark$  v<sub>2</sub> vs. p<sub>T</sub> that would be obtained from 2.10<sup>7</sup> semi-peripheral events (6<b<9)



p <sub>T</sub> limits	$N(D^{\pm})_{sel}$	<b>σ</b> (v <sub>2</sub> )
0-0.5	645	0.03
0.5-1	1290	0.02
1-1.5	1800	0.017
1.5-2	1650	0.018
2-3	2470	0.015
3-4	1160	0.02
4-8	1225	0.02
8-15	220	0.05

## **Glauber calculations (I)**

• N-N c.s.:

 $\sigma_{NN}^{inel} = 60 \, mb$  $\sigma_{NN}^{c\bar{c}} = 6.64 \, mb$ 

- $\sigma^{cc}$  from HVQMNR
- + shadowing
- Pb Woods-Saxon

$$\rho(r) = \frac{\rho_0}{1 + e^{\frac{r - r_0}{d}}}$$

$$\rho_0 = 0.16 \ fm^{-3}$$

$$r_0 = 6.624 \ fm$$

$$d = 0.549 \ fm$$



## **Glauber calculations (II)**

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$$r_0 = 6.624 \ fm$$

$$d = 0.549 \ fm$$



## Shadowing parametrization



<sup>1</sup> Eskola et al., Eur. Phys. J C 9 (1999) 61.

Emel'yanov et al., Phys. Rev. C 61 (2000) 044904.

## **Effect of charm mass at the LHC**















- At t=0: geometrical anisotropy (almond shape), momentum distribution isotropic
  - Interaction among consituents generate a pressure gradient which transform the initial spatial anisotropy into a momentum anisotropy
    - Multiple interactions lead to thermalization → limiting behaviour = ideal hydrodynamic flow
  - The mechanism is self quenching
    - The driving force dominate at early times
    - Probe Equation Of State at early times

# $\frac{dX}{d\varphi} = \frac{X_0}{2\pi} (1 + 2v_1 \cos(\varphi - \Psi_{RP}) + \frac{v_2}{v_2} \cos(2(\varphi - \Psi_{RP})) + ....)$







## "Glauber" calculations

Optical approximation

Czyz and Maximon, Annals Phys. 52 (1969) 59.

Nucleus thickness  
functions
$$T_{A}(\vec{s}) = \int_{-\infty}^{\infty} \rho_{A}(\vec{s}, z_{A}) dz_{A} T_{B}(\vec{s} - \vec{b}) = \int_{-\infty}^{\infty} \rho_{B}(\vec{s} - \vec{b}, z_{B}) dz_{B}$$
Nucleus-nucleus  
thickness function
$$T_{AB}(\vec{b}) = \int T_{A}(\vec{s}) T_{B}(\vec{s} - \vec{b}) ds^{2}$$
Nucleon-nucleon  
collision probability
$$P(1, \vec{b}) = T_{AB}(\vec{b}) \sigma_{in} \rightarrow P(n, \vec{b}) = {AB \choose n} (T_{AB}(\vec{b}) \sigma_{in})^{n} (1 - T_{AB}(\vec{b}) \sigma_{in})^{AB-n}$$

Part = 
$$\int \{A T_A[1 - (1 - \sigma_{in} T_B)^B] + B T_B[1 - (1 - \sigma_{in} T_A)^A]\} ds^2$$

$$\rightarrow$$
 Coll = A B T<sub>AB</sub>  $\sigma_{in}$ 

## **Event plane simulation**

• Simple generation of particle azimuthal angles ( $\phi$ ) according to a probability distribution

$$\frac{dN}{d\boldsymbol{\varphi}} = 1 + 2v_2 \cos(\boldsymbol{\varphi} - \boldsymbol{\Psi}_{RP})$$

- Faster than complete AliRoot generation and reconstruction
- Results compatible with the ones in PPR chapter 6.4



